



# Climate Predictions with imperfect models

("Hadley Centre QUMP")

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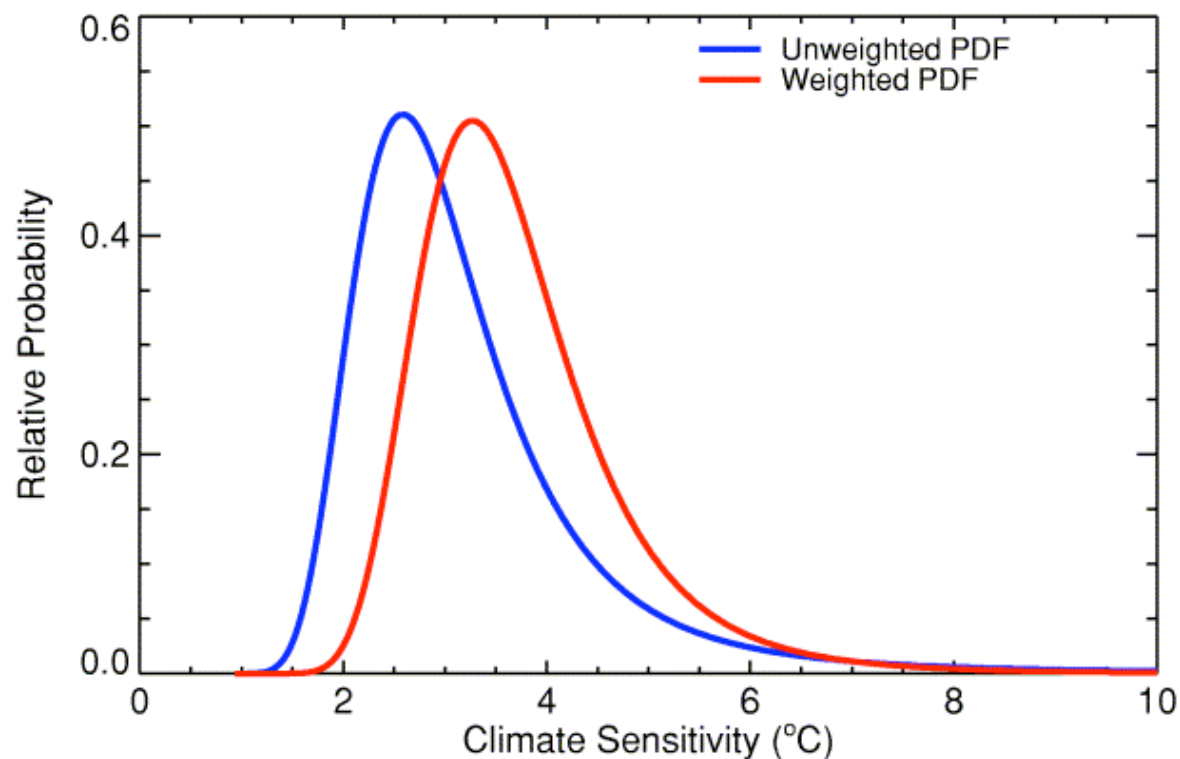
1.Introduction

2.Bayesian framework

3.Estimating model imperfection

4.Conclusions

# Probabilistic predictions



Murphy et al 2004

Red curve calculated by weighting different parts of parameter space according to quality of simulation of present-day climate

# What does probability distribution mean



- Could give policy-maker terabytes of model and observed data each time
- OR a summary statement of how future climate is consistent with the information provided
- Probability distribution is a function of
  - Model data
  - Observations
  - Prior information
  - Model imperfections
  - Analysis method and assumptions

- Compare models against several observational variables – with just one variable you can simulate climate well for the wrong reasons
- Will compare with present-day mean climate - Indirect assessment of key processes for our climate prediction but adds confidence to our prediction of one-off event
- We are not going to assume models are perfect so using better models has an impact

# Bayesian framework

- Aim is to construct joint probability distribution  $p(X, m_h, m_f, y, o, d)$  of all uncertain objects in problem.
  - Input parameters (X)
  - Historical Model output ( $m_h$ )
  - Model prediction ( $m_f$ )
  - True climate ( $y_h, y_f$ )
  - Observations (o)
  - Model imperfections (d)
- It measures how all objects are related in a probabilistic sense

# Goldstein and Rougier (2004) – The “Best-input” assumption



- Start with a perturbed physics ensemble
- Hypothesise that there is a set of input parameters,  $x^*$ , that provide the best climate model
- But acknowledge that this best model is imperfect and that there is a **discrepancy**,  $d$ , compared to real climate
- We only know the probability that each point in parameter space is the best-input model. But that means we need a model at every part of parameter space...

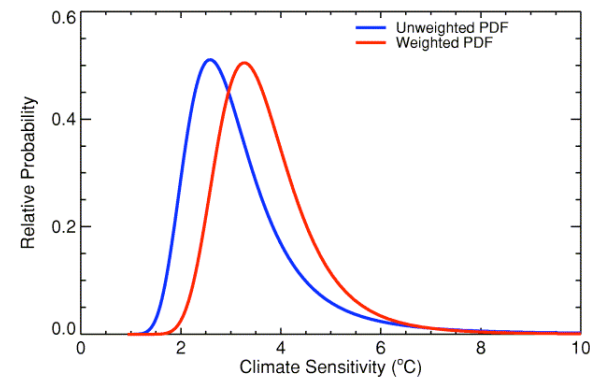
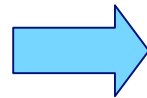
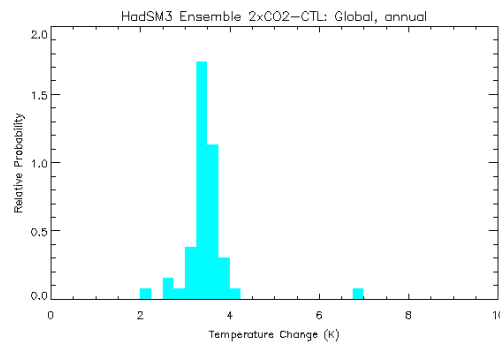


# Emulators



Emulators are statistical models, trained on ensemble of 300 slab runs, designed to predict model output at untried parameter combinations (a t-distribution at each sampled point)

Monte Carlo sampling of parameters combined with an emulator (combining lots of t-distributions) produces prior pdf (blue line).



# Linking objects in Bayesian framework



Climate model

Discrepancy

True  
climate

$$y = f(x^*) + \varepsilon$$

Observations

$$o = y_h + e$$

Emulator

Model

$$f(x) = \mu(x) + u(x)$$

$$o = \mu_h(x^*) + u_h(x^*) + \varepsilon_h + e$$

Emulator  
error

Discrepancy

Obs error

# Comparing models with observations



- Use likelihood function i.e. skill of model is likelihood of model data given some observations

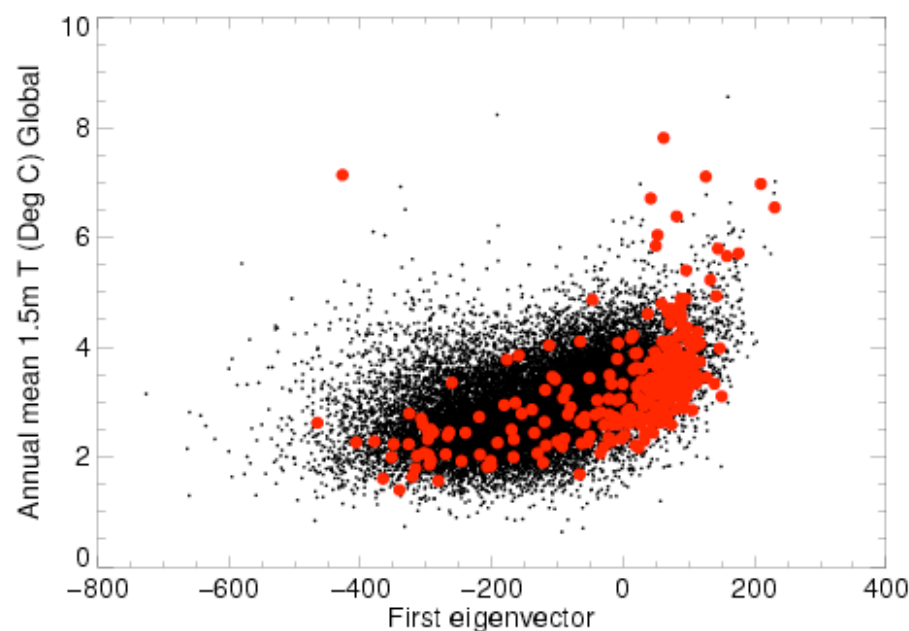
$$\log L_o(\mathbf{m}) = -c - \frac{n}{2} \log |\mathbf{V}| - \frac{1}{2} (\mathbf{m} - \mathbf{o})^T \mathbf{V}^{-1} (\mathbf{m} - \mathbf{o})$$

$\mathbf{V}$  = obs uncertainty + emulator error + discrepancy

# Constraining predictions



- Likelihood alters probability of  $x^*$
- Reduce uncertainty about the best input,  $x^*$



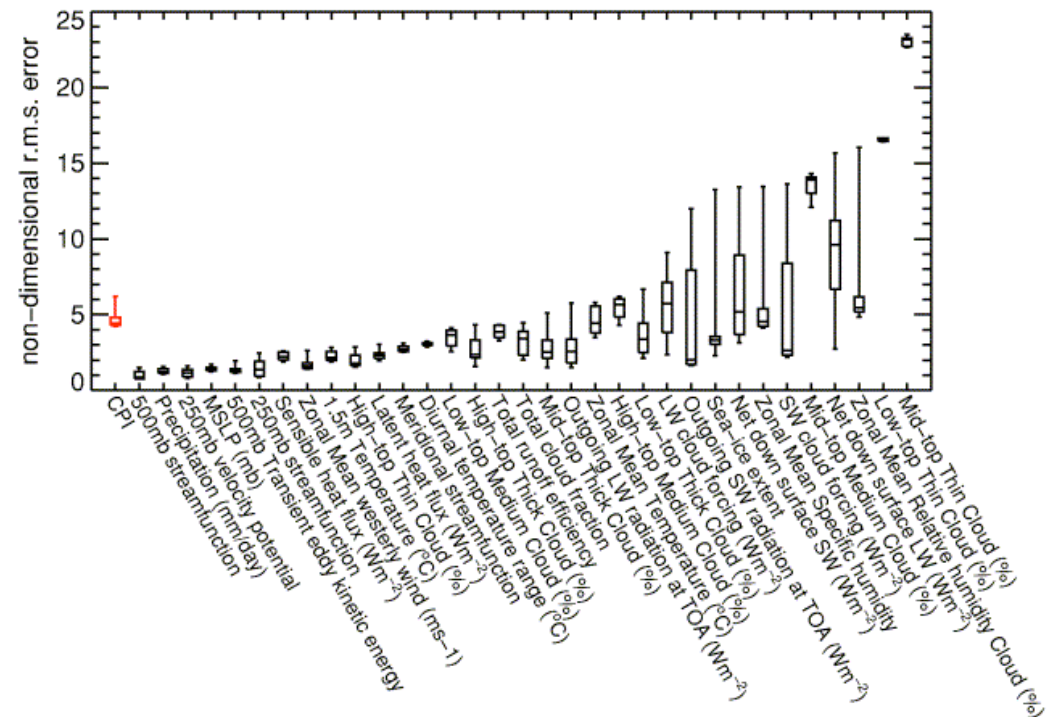
- Most effective if a strong relationship exists

- Model not perfect so there are processes in real system not in our model that could alter model response by an uncertain amount.
- Places extra uncertainty on prediction variable in form of a variance

# Discrepancy (ii)



- Avoids observations over-constraining the pdfs.
- Avoids contradictions from subsequent analyses when some observations have been allowed to constrain the problem too strongly.



- Provides a means of accounting for model quality
  - Models with less imperfection given more weight – dynamics/physics matter!
  - Model improvements can subsequently be tracked
  - Constraint of observations gradually improve as model improves rather than jumping from “unusable” to “usable”.

Estimating a proxy for discrepancy



- Four ways I can think of...
  - Elicitation
  - Observations
  - Super-parameterised models
  - Ensemble of international climate models

- Use multimodel ensemble from AR4 and CFMIP
- For each multimodel ensemble member, find point in QUMP parameter space that is closest to that member
- There is a distance between climates of this multimodel ensemble member and this point in parameter space i.e. effect of processes not explored by QUMP.
- Pool these distances over all multimodel ensemble members

# Adding information from other climate models e.g. summer UK rainfall

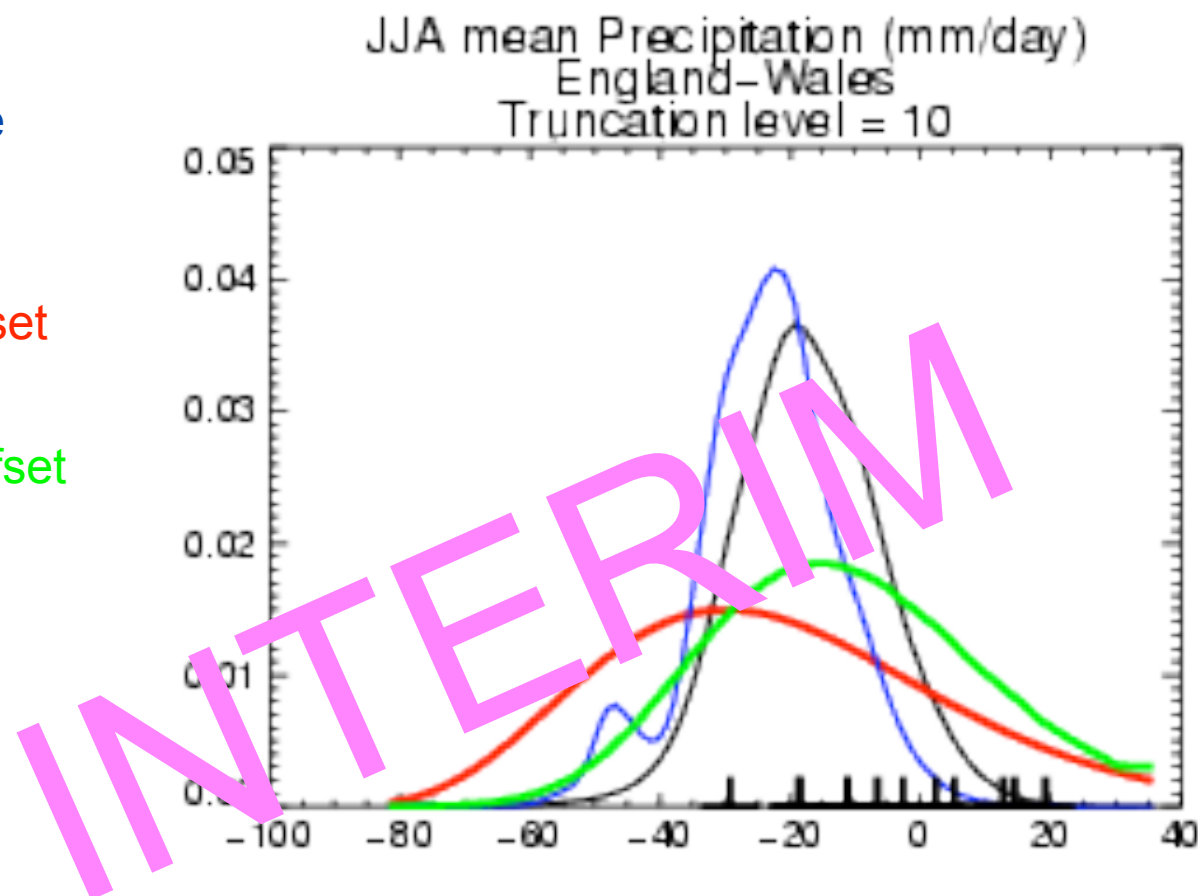


Prior

Posterior - no future  
discrepancy

Posterior – future  
discrepancy, no offset

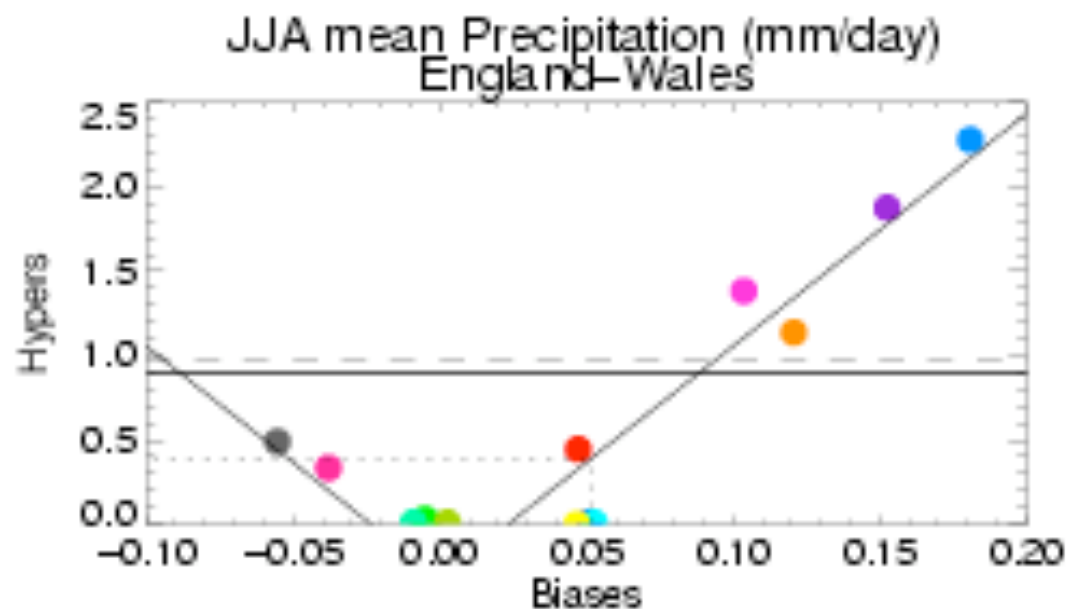
Posterior – future  
discrepancy with offset



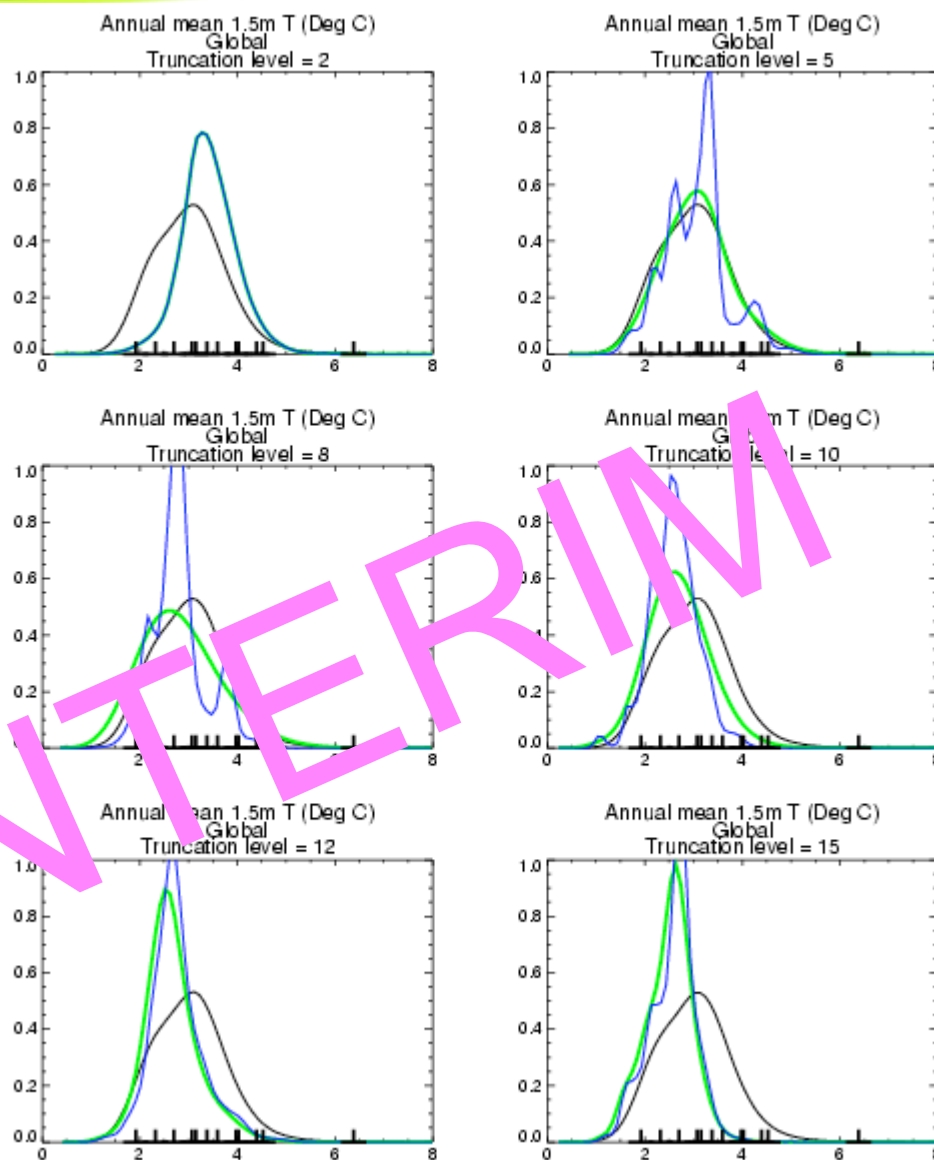
# Biases in QUMP prediction of multimodel runs



X-axis is difference  
between each multimodel  
and its 'best point' in  
QUMP parameter space



# Climate sensitivity



# Conclusions

## ■ MULTIVARIATE

- Predicts joint distributions
  - Predictions of individual variables consistent with marginal distributions from joint analysis
  - Different prediction variables can be constrained by different observations
- Can use lots of observations to constrain prediction
  - Only new independent observations impact on probability distribution

## ■PRIOR

- Don't let predictions be dependent on sampling strategy
- Instead predictions are representative of whole parameter space given some expert-chosen distribution
- Allow a sensitivity analysis so it is easy to try out different expert's distributions



## ■ MODEL IMPERFECTIONS

- Acknowledge that our models are not perfect therefore we have to be careful about comparing modelled and observed data
  - Don't let poorly modelled variables over-constrain PDF
- Allow for a modelling uncertainty additional to one explored by perturbing parameters:
  - Observable model variables
  - Forecast variables

- Improve observational uncertainties
- Improve model i.e. reduce discrepancy
- Run larger ensembles
- Use more observational constraints independent of the ones used already

- Please keep producing better data sets that allow the model to be evaluated in more detail
- Require observational errors in an easily-accessible format
- Any advice on errors for ERBE, CERES, or ISCCP most welcome.
- Any advice most welcome on new data sets and whether they need new model diagnostics.